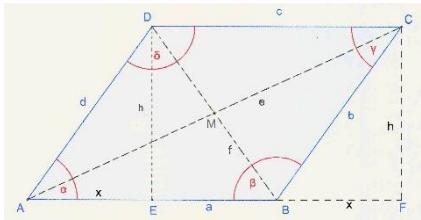


Trigonometrie – Berechnungen im Parallelogramm und Trapez

Lösungsblatt

Berechnen Sie in folgenden Beispielen die gesuchten Größen!



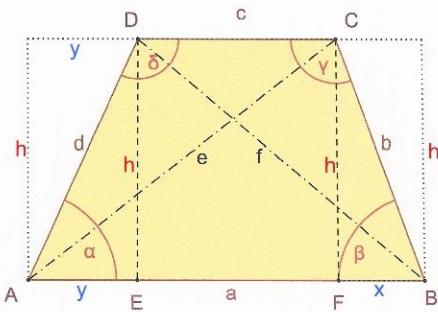
$$\begin{aligned} h^2 &= e^2 - (a+x)^2 \quad \text{und} \quad h^2 = f^2 - (a-x)^2 \\ &\rightarrow h^2 = h^2 \\ e^2 - (a+x)^2 &= f^2 - (a-x)^2 \end{aligned}$$

$$\begin{aligned} e^2 - (a+x)^2 &= f^2 - (a-x)^2 \\ e^2 - a^2 - 2ax - x^2 &= f^2 - a^2 + 2ax - x^2 \\ e^2 - f^2 &= 4ax \\ x = \frac{e^2 - f^2}{4a} &\rightarrow x = \frac{123^2 - 71^2}{4 \cdot 80} \\ x &= 31,525 \text{ m} \end{aligned}$$

Parallelogramm ABCD: $a = 80 \text{ m}$, $e = 123 \text{ m}$, $f = 71 \text{ m}$;
Zu berechnen sind: h , b , U , A , $\alpha = \gamma$ und $\beta = \delta$!

$$\begin{aligned} h^2 &= e^2 - (a+x)^2 \\ h^2 &= 123^2 - 111,525^2 \\ h &= \sqrt{2691,174375} \\ h &= 51,876 \text{ m} \\ b^2 &= h^2 + x^2 \\ b^2 &= 51,876^2 + 31,525^2 \\ b &= \sqrt{3685} \\ b &= 60,704 \text{ m} \\ U &= 2 \cdot (a+b) \\ U &= 2 \cdot (80 + 60,704) \\ U &= 281,408 \text{ m} \end{aligned}$$

$$\begin{aligned} A &= a \cdot h \\ A &= 80 \cdot 51,876 \\ A &= 4150,08 \text{ m}^2 \\ \sin \alpha &= \frac{h}{b} \\ \sin \alpha &= \frac{51,876}{60,704} \\ \sin \alpha &= 0,8545\dots \\ \alpha &= 58,71^\circ = \gamma \\ \beta &= 180^\circ - \alpha \\ \beta &= 180^\circ - 58,71^\circ \\ \beta &= 121,29^\circ = \delta \end{aligned}$$



$$\begin{aligned} h^2 &= b^2 - x^2 \quad \text{und} \quad h^2 = e^2 - (a-x)^2 \\ &\rightarrow h^2 = h^2 \\ b^2 - x^2 &= e^2 - (a-x)^2 \end{aligned}$$

$$\begin{aligned} b^2 - x^2 &= e^2 - (a-x)^2 \\ b^2 - x^2 &= e^2 - a^2 + 2ax - x^2 \\ b^2 - e^2 + a^2 &= 2ax \\ x = \frac{b^2 - e^2 + a^2}{2a} &\rightarrow x = \frac{59^2 - 88^2 + 90^2}{2 \cdot 90} \\ x = \frac{3837}{180} &\rightarrow x = 21,32 \text{ m} \end{aligned}$$

Trapez ABCD: $a = 90 \text{ m}$, $b = 59 \text{ m}$, $c = 45 \text{ m}$, $e = 88 \text{ m}$;
Zu berechnen sind: h , d , α , β , γ , δ , U und A !

$$\begin{aligned} h^2 &= b^2 - x^2 \\ h^2 &= 59^2 - 21,32^2 \\ h &= \sqrt{3026,59} \\ h &= (\sim) 55 \text{ m} \\ y &= a - x - c \\ y &= 90 - 21,32 - 45 \\ y &= 23,68 \text{ m} \\ d^2 &= h^2 + y^2 \\ d^2 &= 55^2 + 21,32^2 \\ d &= \sqrt{3585,742} \\ d &= 59,88 \text{ m} \end{aligned}$$

$$\begin{aligned} \sin \alpha &= \frac{h}{d} & \sin \beta &= \frac{h}{b} \\ \sin \alpha &= \frac{55}{59,88} & \sin \beta &= \frac{55}{59} \\ \sin \alpha &= 0,9185\dots & \sin \beta &= 0,9322\dots \\ \alpha &= 66,71^\circ & \beta &= 68,78^\circ \\ \delta &= 180^\circ - \alpha & \delta &= 180^\circ - \beta \\ \delta &= 180^\circ - 66,71^\circ & \delta &= 180^\circ - 68,78^\circ \\ \delta &= 113,29^\circ & \delta &= 111,22^\circ \\ U &= a + b + c + d & A &= \frac{1}{2} \cdot (a+c) \cdot h \\ U &= 90+59+45+59,88 & A &= \\ U &= 253,88 \text{ m} & A &= \frac{1}{2} \cdot (90+45) \cdot 55 \\ & & A &= 3712,5 \text{ m}^2 \end{aligned}$$